

Precalculus Warm-Up - Section 5.1 and 5.2

Match the function with one of the following.

- (a) $\sec^2 x \csc^2 x$ (b) $\sec x + \tan x$ (c) $2\sec^2 x$
 (d) $\tan x \sin x$ (e) $\sin x \cos x$

1) $(1 + \sec x)(1 - \cos x)$

1) d

$$1 - \cos x + \sec x - 1$$

$$\frac{\sec x - \cos x}{\cos x} = \frac{1 - \cos^2 x}{\cos x} = \frac{\sin^2 x}{\cos x} = \tan x \sin x$$

2) $\sec^2 x + \csc^2 x$

2) a

$$\frac{1}{\cos^2 x} + \frac{1}{\sin^2 x} = \frac{\sin^2 x + \cos^2 x}{\cos^2 x \sin^2 x} = \frac{1}{\cos^2 x \sin^2 x} = \sec^2 x \csc^2 x$$

3) $\frac{1}{1 + \sin x} + \frac{1}{1 - \sin x}$

3) c

$$\frac{1 - \sin x + 1 + \sin x}{1 - \sin^2 x} = \frac{2}{\cos^2 x} = 2\sec^2 x$$

4) $\frac{1}{\tan x + \cot x}$

4) e

$$\frac{1}{\frac{\sin x}{\cos x} + \frac{\cos x}{\sin x}} = \frac{1}{\frac{\sin^2 x + \cos^2 x}{\sin x \cos x}} = 1 \cdot \frac{\sin x \cos x}{1}$$

5) $\frac{\cos x}{1 - \sin x}$

5) b

$$\frac{\cos x}{1 - \sin x} \cdot \frac{1 + \sin x}{1 + \sin x} = \frac{\cos x(1 + \sin x)}{1 - \sin^2 x}$$

$$\frac{\cos x(1 + \sin x)}{\cos^2 x} = \frac{1 + \sin x}{\cos x} = \sec x + \tan x$$

