

AP MC Opener 7.2

Name _____

1. Evaluate: $\int x^2 \sin(x^3) dx$

$$u = x^3 \quad \frac{du}{dx} = 3x^2$$

$$du = 3x^2 dx \quad \frac{1}{3} du = x^2 dx$$

A) $-\frac{x^3}{3} \cos\left(\frac{x^4}{4}\right) + C$

B) $-\frac{1}{3} \cos(x^3) + C$

C) $\frac{1}{3} \cos(x^3) + C$

D) $-3 \cos(x^3) + C$

E) $-\frac{1}{3} \sin(x^3) + C$

$$\frac{1}{3} \int \sin u du$$

$$= -\frac{1}{3} \cos(x^3) + C$$

2. Evaluate: $\int_1^3 \frac{x}{x^2+1} dx$

$$u = x^2 + 1$$

$$\frac{du}{dx} = 2x$$

$$\frac{1}{2} du = x dx$$

$$u(1) = 2 \quad u(3) = 10$$

A) $\ln 5$

B) $\ln 10$

C) $2 \ln 2$

D) $\frac{1}{2} \ln 5$

E) $\ln\left(\frac{5}{2}\right)$

$$\frac{1}{2} \int_2^{10} \frac{1}{u} du = \frac{1}{2} (\ln 10 - \ln 2)$$

$$= \frac{1}{2} \ln 5$$