

Let's consider $f(x) = x^3 - 5x + 1$:

- a. Find $f(2)$:
b. Find $f(2.1)$:
c. Find the equation of the tangent line to $f(x)$ at $x=2$.
d. Using the tangent line find the value of y when $x = 2.1$.
e. Now compare your results for b and d. Are the values close?

Given $f(4) = 2$ and $f'(4) = -3$, Estimate $f(4.01)$.

Let's consider $f(x) = x^3 - 5x + 1$:

- a. Find $f(2)$: -1
b. Find $f(2.1)$: $-.239$

- c. Find the equation of the tangent line to $f(x)$ at $x=2$. *point (2, -1) slope = $f'(2)$*

$$f'(x) = 3x^2 - 5$$

$$f'(2) = 3(2)^2 - 5 = 7$$

$$y + 1 = 7(x - 2) \Rightarrow \boxed{y = 7(x - 2) - 1}$$

- d. Using the tangent line find the value of y when $x = 2.1$.

$$y + 1 = 7(2.1 - 2)$$
$$y = 7(2.1 - 2) - 1 = -.3 \text{ Yes!}$$

- e. Now compare your results for b and d. Are the values close?

Yes! Good estimate.

Given $f(4) = 2$ and $f'(4) = -3$, Estimate $f(4.01)$.

point
 $(4, 2)$

slope @ $x=4$
 $= -3$

$$y - 2 = -3(x - 4)$$

$$y = -3(4.01 - 4) + 2 = 1.97$$