

$$(4) y = \tan(2x - x^3) \quad u = 2x - x^3$$

$$\frac{dy}{dx} = \sec^2(2x - x^3) \cdot (2 - 3x^2)$$

$$= (2 - 3x^2) \sec^2(2x - x^3)$$

$$(6) y = 5 \cot\left(\frac{z}{x}\right) \quad u = \frac{z}{x} = 2x^{-1}$$

$$\begin{aligned} \frac{dy}{dx} &= -5 \csc^2\left(\frac{z}{x}\right) \cdot (-2x^{-2}) \\ &= \frac{10 \csc^2\left(\frac{z}{x}\right)}{x^2} \end{aligned}$$

$$(7) y = \cos(\sin x) \quad u = \sin x$$

$$\begin{aligned} \frac{dy}{dx} &= -\sin(\sin x) \cdot \cos x \\ &= -\cos x \sin(\sin x) \end{aligned}$$

$$(12) s = \sin\left(\frac{3\pi}{2}t\right) + \cos\left(\frac{7\pi}{4}t\right)$$

$$\begin{aligned} v(t) &= s'(t) = \cos\left(\frac{3\pi}{2}t\right) \cdot \frac{3\pi}{2} - \sin\left(\frac{7\pi}{4}t\right) \cdot \frac{7\pi}{4} \\ &= \frac{3\pi}{2} \cos\left(\frac{3\pi}{2}t\right) - \frac{7\pi}{4} \sin\left(\frac{7\pi}{4}t\right) \end{aligned}$$

$$(16) y = x^3 (2x - 5)^4 \quad \begin{array}{l} \text{(1) Product Rule} \\ \text{(2) Chain rule for } v' \text{ only} \end{array}$$

$$\begin{aligned} \frac{dy}{dx} &= 3x^2 (2x - 5)^4 + x^3 \cdot 4(2x - 5)^3 \cdot 2 \\ &= 3x^2 (2x - 5)^4 + 8x^3 (2x - 5)^3 \end{aligned}$$

$$(20) y = \frac{x}{\sqrt{1+x^2}} \quad \begin{array}{l} \text{(1) Quotient Rule} \\ \text{(2) Chain rule for } v' \text{ only} \end{array}$$

$$\frac{dy}{dx} = \frac{\sqrt{1+x^2} \cdot 1 - x \cdot \frac{1}{2}(1+x^2)^{-\frac{1}{2}} \cdot 2x}{(\sqrt{1+x^2})^2}$$

$$(24) y = \sqrt{\tan 5x} = (\tan 5x)^{\frac{1}{2}}$$

Outermost function  $(\ )^{\frac{1}{2}}$   
middle function  $\tan(\ )$   
innermost function  $5x$

$$\begin{aligned} \frac{dy}{dx} &= \frac{1}{2} (\tan 5x)^{\frac{1}{2}} \cdot \sec^2 5x \cdot 5 \\ &= \frac{5}{2} (\tan 5x)^{\frac{1}{2}} \cdot \sec^2(5x) \end{aligned}$$

$$\begin{aligned} &= \frac{\sqrt{1+x^2} - x^2(1+x^2)^{-\frac{1}{2}}}{1+x^2} \\ &\text{Lots of simplifying!} \end{aligned}$$

$$\frac{\sqrt{1+x^2}}{\sqrt{1+x^2}} = \frac{\sqrt{1+x^2} - \frac{x^2}{\sqrt{1+x^2}}}{1+x^2}$$

$$= \frac{1+x^2-x^2}{\sqrt{1+x^2}} \cdot \frac{1}{1+x^2}$$

$$= \frac{1}{(1+x^2)\sqrt{1+x^2}} = \frac{1}{(1+x^2)^{\frac{3}{2}}}$$

$$(28) r = 2\theta \sqrt{\sec \theta} \quad \begin{array}{l} \text{(1) Product Rule} \\ \text{(2) Chain Rule only for } v' \end{array}$$

$$\begin{aligned} \frac{dr}{d\theta} &= \frac{u'}{2\sqrt{\sec \theta}} + \frac{u}{2\theta} \cdot \frac{1}{2} (\sec \theta)^{-\frac{1}{2}} \cdot \sec \theta \tan \theta \\ &= \frac{1}{2\sqrt{\sec \theta}} + \theta (\sec \theta)^{\frac{1}{2}} \tan \theta \\ &= \frac{1}{\sqrt{\sec \theta}} (2 + \theta \tan \theta) \end{aligned}$$

$$(32) y = 9 \tan\left(\frac{x}{3}\right)$$

$$y' = 9 \sec^2\left(\frac{x}{3}\right) \cdot \left(\frac{1}{3}\right)$$

$$y' = 3 \sec^2\left(\frac{x}{3}\right) \quad \text{Outermost } (\ )^2$$

$$\begin{aligned} y'' &= 3 \cdot 2 \sec\left(\frac{x}{3}\right) \cdot \sec\left(\frac{x}{3}\right) \tan\left(\frac{x}{3}\right) \cdot \frac{1}{3} \sec\left(\frac{x}{3}\right) \\ &= \frac{6 \sec^2\left(\frac{x}{3}\right) \tan\left(\frac{x}{3}\right)}{3} \end{aligned}$$

$$= \boxed{\sqrt{\sec \theta (2 + \theta \tan \theta)}}$$

↑  
GCF

$$y = 3 \cdot 2 \sec\left(\frac{x}{3}\right) \cdot \sec\left(\frac{x}{3}\right) \tan\left(\frac{x}{3}\right) \cdot \frac{1}{3} \sec(1)$$

innermost  
 $\frac{x}{3}$

$$= \boxed{2 \sec^2\left(\frac{x}{3}\right) \tan\left(\frac{x}{3}\right)}$$