

1. $f(x) = \cos\left(\frac{1}{x}\right)$

a) $\lim_{x \rightarrow \infty} f(x) = 1$

b) $\lim_{x \rightarrow -\infty} f(x) = 1$

c) HA $y = 1$

2. $f(x) = \frac{\sin 2x}{x}$

a) $\lim_{x \rightarrow \infty} f(x) = 0$

b) $\lim_{x \rightarrow -\infty} f(x) = 0$

c) HA $y = 0$

4. $f(x) = \frac{3x^3 - x + 1}{x + 3}$

a) $\lim_{x \rightarrow \infty} f(x) = \infty$

b) $\lim_{x \rightarrow -\infty} f(x) = \infty$

c) none

5. $f(x) = \frac{3x+1}{|x|+2}$

a) $\lim_{x \rightarrow \infty} f(x) = 3$

b) $\lim_{x \rightarrow -\infty} f(x) = -3$

c) HA @ $y = 3, y = -3$

13. $\lim_{x \rightarrow 2^+} \frac{1}{x-2} = \infty$

16. $\lim_{x \rightarrow -3^+} \frac{x}{x+3} = -\infty$

21. $y = \left(2 - \frac{x}{x+1}\right) \left(\frac{x^2}{5+x^2}\right)$

$\lim_{x \rightarrow \infty} y = \left[\lim_{x \rightarrow \infty} 2 - \lim_{x \rightarrow \infty} \frac{x}{x+1} \right] \left[\lim_{x \rightarrow \infty} \frac{x^2}{5+x^2} \right]$

$= [2 - 1][1] = 1$

$\lim_{x \rightarrow -\infty} y = \text{same} = 1$

24. $y = \frac{2x + \sin x}{x}$

$\lim_{x \rightarrow \infty} y = \lim_{x \rightarrow \infty} \frac{2x}{x} + \lim_{x \rightarrow \infty} \frac{\sin x}{x}$

$= 2 + 0 = 2$

$\lim_{x \rightarrow -\infty} y = \text{same} = 2$

27. $f(x) = \frac{1}{x^2 - 4} = \frac{1}{(x+2)(x-2)}$

a) V.A. $x = -2, x = 2$

b) $\lim_{x \rightarrow -2^-} f(x) = \infty$ $\lim_{x \rightarrow -2^+} f(x) = -\infty$

$\lim_{x \rightarrow 2^-} f(x) = -\infty$ $\lim_{x \rightarrow 2^+} f(x) = \infty$

29. $f(x) = \frac{x^2 - 2x}{x+1} = \frac{x(x-2)}{x+1}$

a) V.A. $x = -1$

b) $\lim_{x \rightarrow -1^-} f(x) = -\infty$ $\lim_{x \rightarrow -1^+} f(x) = \infty$

31. $f(x) = \cot(x)$

a) V.A. $x = k\pi$,
 k is any integer



k is any integer

$$b) \lim_{x \rightarrow k\pi^-} f(x) = -\infty \quad \lim_{x \rightarrow k\pi^+} f(x) = \infty$$