

$$28. \lim_{x \rightarrow 0} \frac{\frac{1}{2+x} - \frac{1}{2}}{x} = \lim_{(2+x) \rightarrow 0} \frac{2 - (2+x)}{x(2)(2+x)} = \lim_{x \rightarrow 0} \frac{-x}{2x(2+x)} = \lim_{x \rightarrow 0} \frac{-1}{2(2+x)} = \boxed{\frac{-1}{4}}$$

$$30. \lim_{x \rightarrow 0} \frac{\sin 2x}{x} \cdot \frac{2}{2} = \lim_{x \rightarrow 0} 2 \cdot \frac{\sin 2x}{2x} = 2 \cdot 1 = \boxed{2}$$

$$31. \lim_{x \rightarrow 0} \frac{\sin x}{2x^2 - x} = \lim_{x \rightarrow 0} \frac{\sin x}{x} \cdot \frac{1}{2x-1} = 1 \cdot \frac{1}{-1} = \boxed{-1}$$

$$33. \lim_{x \rightarrow 0} \frac{\sin^2 x}{x} = \lim_{x \rightarrow 0} \frac{\sin x}{x} \cdot \sin x = 1 \cdot 0 = \boxed{0}$$

43. See Q.1 day 1

- | | |
|------|------|
| a) T | b) F |
| c) F | d) T |
| e) T | f) T |
| g) T | |
| h) T | |
| i) T | |

$$55. a) \lim_{x \rightarrow 4} (g(x) + 3) = \lim_{x \rightarrow 4} g(x) + \lim_{x \rightarrow 4} 3 \\ = 3 + 3 = \boxed{6}$$

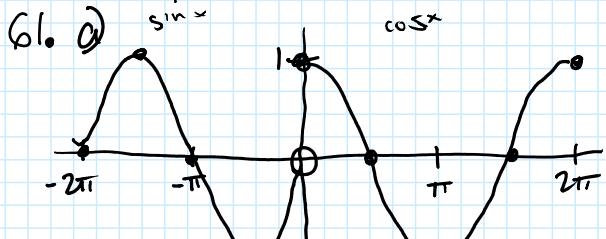
$$b) \lim_{x \rightarrow 4} f(x) = \lim_{x \rightarrow 4} x \cdot \lim_{x \rightarrow 4} f(x) \\ = 4 \cdot 0 = \boxed{0}$$

$$c) \lim_{x \rightarrow 4} g^2(x) = (\lim_{x \rightarrow 4} g(x))^2 = (3)^2 = \boxed{9}$$

$$d) \lim_{x \rightarrow 1} \frac{g(x)}{f(x)-1} = \frac{3}{0-1} = \boxed{-3}$$

56. a) 4
 b) -21
 c) -12
 d) $-\frac{7}{3}$

$$61. a) \frac{\sin x}{x} \quad | \quad \frac{\cos x}{x}$$



- b) $(-2\pi, 0) \cup (0, 2\pi)$ $\liminf_{x \rightarrow c} f(x)$ exists
c) 2π L.H.
d) -2π R.H.

71. True - definition of limit.

$$72. \text{ True: } \lim_{x \rightarrow 0} \frac{x + \sin x}{x} = \lim_{x \rightarrow 0} \frac{x}{x} + \lim_{x \rightarrow 0} \frac{\sin x}{x} = 1 + 1 = \boxed{2}$$

73. C

74. B

75. E

76. C